STRANGE PRODUCTIONS THROUGH TRANSPORT APPROACH AT COLLIDING ENERGY $\sqrt{s_{NN}} = 54.4 \text{ GeV/A}$

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OUTLINE

✓ PROBING RELATIVISTIC NUCLEAR COLLISIONS THROUGH STRANGE PRODUCTIONS

 ✓ STUDYING STRANGENESS USING TRANSPORT APPROACH-MOMENTUM INTEGRATED BOLTZMANN EQUATION

- ✓ FORMALISM
- ✓ YIELD RATIO PLOTS
- ✓ SUMMARY AND OUTLOOK

QCD PHASE DIAGRAM : SCHEMATIC AND NOT TO SCALE





Introduction

How to know whether the desired system is formed or not?

Answer: > Direct probes > Indirect probes

- \checkmark Dimension of the system formed is very small.
- ✓ Lifetime of system is very small

Hence, Indirect probes are our only recourse





EXPERIMENTS



	Experiments	E _{beam} (A GeV)	$\sqrt{s_{NN}}$ (GeV)	System	Particles
AGS	E802, E866, E877, E891, E895, E917	2-10.7	2.7-4.9	Au+Au	π, K, p, Λ
SPS	NA45, NA49, NA57, (NA44, WA98)	20-158	6.3-17.3	Pb+Pb	π, Κ, p, φ, Λ, Ξ, Ω,
RHIC	STAR, PHENIX, BRAHMS, PHOBOS	-	20.0-200.0	Au+Au	π, Κ, ρ, φ, Λ, Ξ, Ω,

Motivation for Studying Strangeness productions

Why was strangeness thought to be a good probe to diagnose the medium ?

EXPERIMENTAL MOTIVATION BEHIND THE STRANGENESS STUDIES



Importance of K/π ratio

 π is the lightest hadron and is copiously produced in heavy ion collisions. Therefore it is also the measure of entropy of the system

Similarly K is the lightest strange meson and hence representation of strangeness production

Hence Kaon/Pion ratio proposed as measure of strangeness to entropy ratio

STRANGENESS ENHANCEMENT (HIGH DENSITY REGION)



Therefore, it is easier to create $s\bar{s}$ pair than $u\bar{u}$ or dd

K⁺ DISTILLATION (HIGH DENSITY REGION)



List of Major Strange Particles $\Phi(s\overline{s}) K(q\overline{s}) \overline{K}(\overline{q}s) \Xi(qss) \overline{\Xi}(\overline{qss}) \Omega(sss) \overline{\Omega}(\overline{sss})$

- ✓QGP Region is more abundant in u and d quarks than \overline{u} and \overline{d} . \overline{s} and s are equal in number
- Since it is easier to locate u and d than single u, s is more likely to go to Λ(uds) than K⁻(us).

✓Unlike K⁻(us) , K⁺(us) has no competition

Hence, Enhancement of K⁺ > Enhancement of K⁻

WORKING OF OUR MODEL

- Model is developed using Momentum Integrated Boltzmann equation.
- We solve rate equations for all strange degrees of freedoms simultaneously along with temperature and baryon chemical potential.
- Non-strange hadron yields are estimated using thermal model.

ASSUMPTIONS

- We assume that hadronic system is formed after QGP at Tc.
- Non-strange hadrons dominated by pions, are in thermal equilibrium.
- Strange hadrons are slightly away from thermal equilibrium due to their different interaction strength.

RATE EQUATIONS OR MOMENTUM INTEGRATED BOLTZMANN EQUATIONS FOR KAONS

$$\begin{aligned} \frac{dn_{K}}{dt} + \frac{n_{K}}{t} &= n_{\pi}n_{\pi}\langle\sigma v\rangle_{\pi\pi\to K\bar{K}} - n_{K}n_{\bar{K}}\langle\sigma v\rangle_{K\bar{K}\to\pi\pi} + n_{\rho}n_{\rho}\langle\sigma v\rangle_{\rho\rho\to K\bar{K}} - n_{K}n_{\bar{K}}\langle\sigma v\rangle_{K\bar{K}\to\rho\rho} \\ &+ n_{\pi}n_{\rho}\langle\sigma v\rangle_{\pi\rho\to K\bar{K}} - n_{K}n_{\bar{K}}\langle\sigma v\rangle_{K\bar{K}\to\pi\rho} + n_{\pi}n_{N}\langle\sigma v\rangle_{\pi N\to\Lambda K} - n_{\Lambda}n_{K}\langle\sigma v\rangle_{\Lambda K\to\pi N} \\ &+ n_{\rho}n_{N}\langle\sigma v\rangle_{\rho N\to\Lambda K} - n_{\Lambda}n_{K}\langle\sigma v\rangle_{\Lambda K\to\rho N} + n_{\pi}n_{N}\langle\sigma v\rangle_{\pi N\to\Sigma K} - n_{\Sigma}n_{K}\langle\sigma v\rangle_{\Sigma K\to\pi N} \\ &+ n_{\bar{K}}n_{N}\langle\sigma v\rangle_{\bar{K}N\to K\Xi} - n_{K}n_{\Xi}\langle\sigma v\rangle_{K\Xi\to\bar{K}N} + n_{p}n_{\bar{p}}\langle\sigma v\rangle_{p\bar{p}\to K\bar{K}} - n_{K}n_{\bar{K}}\langle\sigma v\rangle_{K\bar{K}\to\rho\bar{p}} \\ &+ n_{\bar{K}}n_{\Lambda}\langle\sigma v\rangle_{\bar{K}\Lambda\to\Omega K} - n_{\Omega}n_{K}\langle\sigma v\rangle_{\Omega K\to\bar{K}\Lambda} + n_{\bar{K}}n_{\Sigma}\langle\sigma v\rangle_{\bar{K}\Sigma\to\Omega K} - n_{\Omega}n_{K}\langle\sigma v\rangle_{\Omega K\to\bar{K}\Sigma} \\ &+ n_{\pi}n_{\Xi}\langle\sigma v\rangle_{\pi\Xi\to K\Omega} - n_{\Omega}n_{K}\langle\sigma v\rangle_{\Omega K\to\pi\Xi} \end{aligned}$$

$$\begin{aligned} \frac{dn_{\bar{K}}}{dt} + \frac{n_{\bar{K}}}{t} &= n_{\pi}n_{\pi}\langle\sigma v\rangle_{\pi\pi\to K\bar{K}} - n_{K}n_{\bar{K}}\langle\sigma v\rangle_{K\bar{K}\to\pi\pi} + n_{\rho}n_{\rho}\langle\sigma v\rangle_{\rho\rho\to K\bar{K}} - n_{K}n_{\bar{K}}\langle\sigma v\rangle_{K\bar{K}\to\rho\rho} \\ &+ n_{\pi}n_{\rho}\langle\sigma v\rangle_{\pi\rho\to K\bar{K}} - n_{K}n_{\bar{K}}\langle\sigma v\rangle_{K\bar{K}\to\pi\rho} - n_{\bar{K}}n_{N}\langle\sigma v\rangle_{\bar{K}N\to\Lambda\pi} + n_{\Lambda}n_{\pi}\langle\sigma v\rangle_{\Lambda\pi\to\bar{K}N} \\ &- n_{\bar{K}}n_{N}\langle\sigma v\rangle_{\bar{K}N\to\Sigma\pi} + n_{\Sigma}n_{\pi}\langle\sigma v\rangle_{\Sigma\pi\to\bar{K}N} - n_{\bar{K}}n_{N}\langle\sigma v\rangle_{\bar{K}N\to K\Xi} + n_{K}n_{\Xi}\langle\sigma v\rangle_{K\Xi\to\bar{K}N} \\ &- n_{\bar{K}}n_{\Lambda}\langle\sigma v\rangle_{\bar{K}\Lambda\to\pi\Xi} + n_{\pi}n_{\Xi}\langle\sigma v\rangle_{\pi\Xi\to\bar{K}\Lambda} - n_{\bar{K}}n_{\Sigma}\langle\sigma v\rangle_{\bar{K}\Sigma\to\pi\Xi} + n_{\pi}n_{\Xi}\langle\sigma v\rangle_{\pi\Xi\to\bar{K}\Sigma} \\ &+ n_{p}n_{\bar{p}}\langle\sigma v\rangle_{p\bar{p}\to K\bar{K}} - n_{K}n_{\bar{K}}\langle\sigma v\rangle_{K\bar{K}\to\rho\bar{p}} - n_{\bar{K}}n_{\Lambda}\langle\sigma v\rangle_{\bar{K}\Lambda\to\Omega K} + n_{\Omega}n_{K}\langle\sigma v\rangle_{\Omega K\to\bar{K}\Lambda} \\ &- n_{\bar{K}}n_{\Sigma}\langle\sigma v\rangle_{\bar{K}\Sigma\to\Omega K} + n_{\Omega}n_{K}\langle\sigma v\rangle_{\Omega K\to\bar{K}\Sigma} \end{aligned}$$

RATE EQUATIONS OR MOMENTUM INTEGRATED BOLTZMANN EQUATIONS FOR HYPERONS

$$\begin{aligned} \frac{dn_{\Lambda}}{dt} + \frac{n_{\Lambda}}{t} &= n_{\pi} n_{N} \langle \sigma v \rangle_{\pi N \to \Lambda K} - n_{\Lambda} n_{K} \langle \sigma v \rangle_{\Lambda K \to \pi N} + n_{\rho} n_{N} \langle \sigma v \rangle_{\rho N \to \Lambda K} - n_{\Lambda} n_{K} \langle \sigma v \rangle_{\Lambda K \to \rho N} \\ &- n_{\Lambda} n_{\Lambda} \langle \sigma v \rangle_{\Lambda \Lambda \to N \Xi} + n_{N} n_{\Xi} \langle \sigma v \rangle_{N \Xi \to \Lambda \Lambda} - n_{\Lambda} n_{\Sigma} \langle \sigma v \rangle_{\Lambda \Sigma \to N \Xi} + n_{N} n_{\Xi} \langle \sigma v \rangle_{N \Xi \to \Lambda \Sigma} \\ &- n_{\bar{K}} n_{\Lambda} \langle \sigma v \rangle_{\bar{K} \Lambda \to \pi \Xi} + n_{\pi} n_{\Xi} \langle \sigma v \rangle_{\pi \Xi \to \bar{K} \Lambda} + n_{\bar{K}} n_{N} \langle \sigma v \rangle_{\bar{K} N \to \Lambda \pi} - n_{\Lambda} n_{\pi} \langle \sigma v \rangle_{\Lambda \pi \to \bar{K} N} \\ &+ n_{p} n_{\bar{p}} \langle \sigma v \rangle_{p \bar{p} \to \Lambda \bar{\Lambda}} - n_{\Lambda} n_{\bar{\Lambda}} \langle \sigma v \rangle_{\Lambda \bar{\Lambda} \to p \bar{p}} + n_{K} n_{\Omega} \langle \sigma v \rangle_{K \Omega \to \bar{K} \Lambda} - n_{\bar{K}} n_{\Lambda} \langle \sigma v \rangle_{\bar{K} \Lambda \to K \Omega} \end{aligned}$$

$$\begin{aligned} \frac{dn_{\Sigma}}{dt} + \frac{n_{\Sigma}}{t} &= n_{\pi} n_{N} \langle \sigma v \rangle_{\pi N \to \Sigma K} - n_{\Sigma} n_{K} \langle \sigma v \rangle_{\Sigma K \to \pi N} - n_{\Lambda} n_{\Sigma} \langle \sigma v \rangle_{\Lambda \Sigma \to N \Xi} + n_{N} n_{\Xi} \langle \sigma v \rangle_{N \Xi \to \Lambda \Sigma} \\ &- n_{\Sigma} n_{\Sigma} \langle \sigma v \rangle_{\Sigma \Sigma \to N \Xi} + n_{N} n_{\Xi} \langle \sigma v \rangle_{N \Xi \to \Sigma \Sigma} - n_{\bar{K}} n_{\Sigma} \langle \sigma v \rangle_{\bar{K} \Sigma \to \pi \Xi} + n_{\pi} n_{\Xi} \langle \sigma v \rangle_{\pi \Xi \to \bar{K} \Sigma} \\ &+ n_{\bar{K}} n_{N} \langle \sigma v \rangle_{\bar{K} N \to \Sigma \pi} - n_{\Sigma} n_{\pi} \langle \sigma v \rangle_{\Sigma \pi \to \bar{K} N} + n_{p} n_{\bar{p}} \langle \sigma v \rangle_{p \bar{p} \to \Sigma \bar{\Sigma}} - n_{\Sigma} n_{\bar{\Sigma}} \langle \sigma v \rangle_{\Sigma \bar{\Sigma} \to p \bar{p}} \\ &+ n_{K} n_{\Omega} \langle \sigma v \rangle_{K \Omega \to \bar{K} \Sigma} - n_{\bar{K}} n_{\Sigma} \langle \sigma v \rangle_{\bar{K} \Sigma \to K \Omega} \end{aligned}$$

RATE EQUATIONS OR MOMENTUM INTEGRATED BOLTZMANN EQUATIONS FOR HYPERONS(Ctd.)

$$\begin{split} \frac{dn_{\Xi}}{dt} + \frac{n_{\Xi}}{t} &= n_{\Lambda} n_{\Lambda} \langle \sigma v \rangle_{\Lambda\Lambda \to N\Xi} - n_{N} n_{\Xi} \langle \sigma v \rangle_{N\Xi \to \Lambda\Lambda} + n_{\Lambda} n_{\Sigma} \langle \sigma v \rangle_{\Lambda\Sigma \to N\Xi} - n_{N} n_{\Xi} \langle \sigma v \rangle_{N\Xi \to \Lambda\Sigma} \\ &+ n_{\Sigma} n_{\Sigma} \langle \sigma v \rangle_{\Sigma\Sigma \to N\Xi} - n_{N} n_{\Xi} \langle \sigma v \rangle_{N\Xi \to \Sigma\Sigma} + n_{\bar{K}} n_{N} \langle \sigma v \rangle_{\bar{K}N \to K\Xi} - n_{K} n_{\Xi} \langle \sigma v \rangle_{K\Xi \to \bar{K}N} \\ &+ n_{\bar{K}} n_{\Lambda} \langle \sigma v \rangle_{\bar{K}\Lambda \to \pi\Xi} - n_{\pi} n_{\Xi} \langle \sigma v \rangle_{\pi\Xi \to \bar{K}\Lambda} + n_{\bar{K}} n_{\Sigma} \langle \sigma v \rangle_{\bar{K}\Sigma \to \pi\Xi} - n_{\pi} n_{\Xi} \langle \sigma v \rangle_{\pi\Xi \to \bar{K}\Sigma} \\ &+ n_{p} n_{\bar{p}} \langle \sigma v \rangle_{p\bar{p} \to \Xi\bar{\Xi}} - n_{\Xi} n_{\bar{\Xi}} \langle \sigma v \rangle_{\Xi\bar{\Xi} \to p\bar{p}} + n_{\Omega} n_{K} \langle \sigma v \rangle_{\Omega K \to \pi\Xi} - n_{\pi} n_{\Xi} \langle \sigma v \rangle_{\pi\Xi \to \Omega K} \end{split}$$

$$\frac{dn_{\Omega}}{dt} + \frac{n_{\Omega}}{t} = n_{p}n_{\bar{p}}\langle\sigma v\rangle_{p\bar{p}\to\Omega\bar{\Omega}} - n_{\Omega}n_{\bar{\Omega}}\langle\sigma v\rangle_{\Omega\bar{\Omega}\to p\bar{p}} + n_{\pi}n_{\Xi}\langle\sigma v\rangle_{\pi\Xi\to\Omega K} - n_{\Omega}n_{K}\langle\sigma v\rangle_{\Omega K\to\pi\Xi}
+ n_{\bar{K}}n_{\Lambda}\langle\sigma v\rangle_{\bar{K}\Lambda\to K\Omega} - n_{K}n_{\Omega}\langle\sigma v\rangle_{K\Omega\to\bar{K}\Lambda} + n_{\bar{K}}n_{\Sigma}\langle\sigma v\rangle_{\bar{K}\Sigma\to K\Omega} - n_{K}n_{\Omega}\langle\sigma v\rangle_{K\Omega\to\bar{K}\Sigma}.$$

The first term in the LHS rate of change of number density, second term is the dilution term due to expansion. Terms in the RHS are the production/annihilation terms.

EVOLUTION OF TEMPERATURE AND CHEMICAL POTENTIAL

Simultaneously, we solve temperature evolution equation,

$$\frac{\partial}{\partial \tau} \left[T^{\frac{4}{(1+c_s^2)}} \tau \right] = 0 \text{ or } T^a \tau = \text{const} = k_2 \text{ and } a = \frac{4}{(1+c_s^2)}$$

We get this following Björken expansion by solving energy momentum conservation equation

$$\partial_{\mu}T^{\mu\nu} = 0$$

Further, the baryon chemical potential equation is solved

$$\partial_{\mu}n_{b}^{\mu}=0$$

IMPORTANCE OF CALCULATION: A MICROSCOPIC APPROACH

This approach takes care of interaction of most probable hadronic channels

The RHS of the rate equation contains the rate of production of species of interest at any time. The rate is give by,

$$\begin{split} \langle \sigma v \rangle &= \frac{T^4}{4} \mathcal{C}_{ab}(T) \int_{z_0}^{\infty} dz [z^2 - (m_a/T + m_b/T)^2] \\ &\times [z^2 - (m_a/T - m_b/T)^2] \sigma K_1(z), \end{split}$$

Sigma is the cross section and v is the relative velocity(Mollar) between two incoming channels. The above expression is for channel $ab \rightarrow cd$

where $C_{ab}(T)$ is given by

$$C_{ab}(T) = \frac{1}{m_a^2 m_b^2 K_2(m_a/T) K_2(m_b/T)}$$
 K₂ is the modified bessel
function of the second kind.
$$z_0 = \max(m_a + m_b, m_c + m_d)/T$$
 17



INTERACTION RATES



INTERACTION RATES



RESULTS



Yield Ratios of Strange Lambdas to Entropy vs. Centrality for Au-Au Collisions at 54.4 AGeV.

SUMMARY AND OUTLOOK

- Yield Ratios of Strange Hadrons to Entropy is measured and plotted at Au-Au Collisions at 54.4 AGeV(Preliminary).
- Efforts have been made to explain the Yield ratio of Lambda to Entropy vs. Centrality using Strange hadron transport model.
- Similar efforts are being made to explain data for other particles like Cascade and Omega.
- Efforts will be made in the future to extend this work to FAIR energies.

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Strangeness production in hadronic scenario

Non linear chiral Lagrangian SU(3)_LxSU(3)_R describing the interaction of pseudo scalar mesons (π , K, η) and baryons; nucleons (N)and Hyperons (Y)

$$\begin{split} L &= \frac{1}{4} f^2 \operatorname{Tr} \partial^{\mu} \Sigma \ \partial_{\mu} \Sigma^{+} + \frac{1}{2} f^2 \Lambda \left[M_q (\Sigma - 1) + h.c. \right] + \operatorname{Tr} \overline{B} \gamma^{\mu} (i \gamma^{\mu} \partial_{\mu} - m_B) B \\ &+ i \operatorname{Tr} \overline{B} \gamma^{\mu} \left[V_{\mu}, B \right] + D \operatorname{Tr} \overline{B} \gamma^{\mu}, \gamma^5 \left[A_{\mu}, B \right] + D \operatorname{Tr} \overline{B} \gamma^{\mu}, \gamma^5 \left[A_{\mu}, B \right] \\ &+ a_1 \operatorname{Tr} \overline{B} \left[\xi M_q \xi + h.c. \right] B + a_2 \operatorname{Tr} \overline{B} B \left[\xi M_q \xi + h.c. \right] + a_3 \operatorname{Tr} \left[M_q \Sigma + h.c. \right] \operatorname{Tr} \overline{B} B \end{split}$$

B is the Baryon Octet with degenerate mass m_B .

G.Q. Li etal. NPA,594(1995)439.

$$\langle I \rangle$$
 $\langle I \rangle$
 π :Pseudo Scalar Meson Octet
f:Pseudo Scalar Meson Decay Constant
 f_{π} = same for all in SU(3)_V Limit=93 MeV

 $\Sigma = \exp\left(\frac{2i\pi}{2}\right), \ \xi = \sqrt{\Sigma} = \exp\left(\frac{i\pi}{2}\right)$

$$V_{\mu} \text{ is the vector meson current and} A_{\mu} \text{ is the axial vector meson current and are given by} V_{\mu} = \frac{1}{2} \Big(\xi^{+} \partial_{\mu} \xi + \xi \ \partial_{\mu} \xi^{+} \Big), A_{\mu} = \frac{i}{2} \Big(\xi^{+} \partial_{\mu} \xi - \xi \ \partial_{\mu} \xi^{+} \Big)$$

 M_q current quark mass matrix with diagonal term = diag $[M_q, M_q, M_s]$, Mass difference between u and d-quarks are neglected

Expanding Σ up to order of $\frac{1}{f^2}$ and keeping explicitly the kaon fields only,

The first two terms in the Lagrangian reduces to

$$\partial^{\mu}\overline{K}\partial_{\mu}K - \Lambda (m_q + m_s)K\overline{K} + \dots$$

where
$$K = \begin{pmatrix} K^+ \\ K^0 \end{pmatrix}$$
, $\overline{K} = \begin{pmatrix} K^- & \overline{K^0} \end{pmatrix}$

..... for other mesons .

For the third and fourth terms in the Lagrangian, when we assume only nucleaon and kaon (KN) interaction, then they reduces to

$$\bar{N}(i\gamma^{\mu}\partial_{\mu}-m_{B})N-\frac{3i}{8f^{2}}\bar{N}\gamma^{0}N\bar{K}\stackrel{\leftrightarrow}{\partial}_{I}K+\cdots,$$

where

..... for other baryons.

$$N = \begin{pmatrix} p \\ n \end{pmatrix}$$
 and $\bar{N} = (\bar{p} \ \bar{n}),$

The last three terms (7th, 8th and 9th) in the Lagrangian reduces to

$$\operatorname{Tr} \bar{B}(\xi M_q \xi + \mathrm{h.c.}) B = 2m_q \bar{N}N - \frac{\bar{N}N}{2f^2}(m_q + m_s) \bar{K}K + \cdots,$$

$$\operatorname{Tr} \bar{B}B(\xi M_q \xi + \mathrm{h.c.}) = 2m_s \bar{N}N - \frac{NN}{f^2}(m_q + m_s)\bar{K}K + \cdots,$$

 $[\operatorname{Tr} M_q \Sigma + \mathrm{h.c.}] \operatorname{Tr} \bar{B}B = 2(2m_q + m_s) \bar{N}N - \frac{2\bar{N}N}{f^2}(m_q + m_s) \tilde{K}K + \cdots$

Scalar attraction for K⁺ and K⁻ Kaplan-Nelson term

Total Lagrangian with

$$\mathcal{L} = \bar{N}(i\gamma^{\mu}\partial_{\mu} - m_{N})N + \partial^{\mu}\bar{K}\partial_{\mu}K - \left(m_{K}^{2} - \frac{\Sigma_{KN}}{f^{2}}\bar{N}N\right)\bar{K}K - \left(m_{K}^{2$$

Weinberg-Tomozawa term

Kaon mass term is given by $m_K^2 = \Lambda(m_q + m_s)$

Nucleon mass term is given by $m_N = m_B - 2[a_1m_q + a_2m_s + a_3(2m_q + m_s)]$ $\Sigma_{KN} \equiv \frac{1}{2}(m_q + m_s) \langle N | \bar{u}u + \bar{s}s | N \rangle = -\frac{1}{2}(m_q + m_s)(a_1 + 2a_2 + 4a_3)$ a_1, a_2 fixed from baryon mass splitting a_3 , uncertain since strangeness content of the nucleon is unknown Hence Σ_{KN} is taken relating to $\Sigma_{\pi N}$ whose value is known (=45 MeV) G. Brown et al., NPA, 596(1996)503: J. Gasser et al. Phys. Lett. B, 253 (1991)252



where s is the square of total c.m. energy, p & p' are 3-momenta of incoming meson & kaon in c.m. frame. M(s,x) is the isospin-averaged squared invariant amplitude.



Isospin averaged cross-section

$$\overline{\sigma}_{\pi N \to AK} = \sum_{i} \frac{2 J_{i} + 1}{(2s_{1} + 1)(2s_{2} + 1)} \frac{\pi}{k_{i}^{2}} \bar{\mathfrak{S}} \frac{B^{in_{i}}B^{out_{i}} \Gamma_{i}^{2}}{\left(s^{1/2} - m_{i}\right)^{2} + \Gamma_{i}^{2}/4}$$

3. BB \rightarrow BYK and others

 $\bullet \ N\,\Delta \to N\,\Lambda\,K \qquad \bullet \Delta\,\Delta \to N\,\Lambda\,K$

• $N N \rightarrow N N K \overline{K}$ • $N N \rightarrow N N \pi \pi K \overline{K}$

Isospin averaged cross section

$$\overline{\sigma}_{NN \rightarrow NAK} = \frac{3 m_n^2}{2 \pi^2 p^2 s} \int_{W_{min}}^{W_{max}} dW W^2 k \int_{q_-^2}^{q_+^2} dq^2 \frac{f_{\pi NN}^2}{m_\pi^2} F^2(q^2) \frac{q^2}{(q^2 - m_\pi^2)^2} \overline{\Rightarrow} \overline{\sigma_0}(W;q^2)$$

$$W_{min} = m_K + m_A$$

$$W_{max} = s^{1/2} - m_N$$

$$q_{\pm}^2 = 2 m_n^2 - 2 E E' \pm 2 p p'$$
while $E = (p^2 + m_N^2)^{1/2}$ & p are the energy & momentum of nucleon N₁ in the c.m. system while E' & p' are those of N₃.
$$F = \frac{\Lambda^2 - m_\pi^2}{\Lambda^2 - q^2}; \Lambda \text{ is the cut off parameter } \Lambda = 1 \text{ GeV}.$$

